On The Edge-face Total Chromatic Number of Pseudo-Halin Graphs with $\Delta(G) \geq 6^1$

LIU Linzhong (Dept. of Management Engineering, Lanzhou Railway Institute, Lanzhou 730070,P.R.China)

Che Qisheng

(Dept. of Mathematics, Gansu TV University, Lanzhou730000,P.R.China) Yang Rongfang

(Dept. of Mathematics, North-west Normal University, Lanzhou 730070, P.R. China)

Abstract: For a 2-connected plane graph G, f_0 is a face without chord on its boundary (a cycle), and all vertices of $V(f_0)$ are at least 3. If remove all edges on the boundary of f_0 , G become a tree T which the degree of vertices except vertices of $V(f_0)$ is at least 3, then G is called a **Pseudo-Halin graph**, G is said to be **Halin graph** if all vertices of $V(f_0)$ is degree 3, and the minimum number $\chi_e(G)$ of colors used to color all elements in $E \cup F$ such that any adjacent or incident elements of $E \cup F$ is colored with distinct color is called **the edge-face total chromatic number of** $G^{[?]}$. In this paper, we have proved that for any Pseudo-Halin graph G with $\Delta(G) \geq 6$, have $\chi_e(G) = \Delta(G)$.

Keywords: Pseudo-Halin graph,edge-face total chromatic number. (AMS1991) 05C15

¹This research is supported by NSFC(No.19871036)